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# Mathematics Colloquium at Jacobs University Bremen

JOHN CREMONA

(University of Warwick, currently at Bristol)

will speak on

*Unimodular Integer Circulants*

**Date:** Monday, November 26, 2007

**Time:** 17:15

**Place:** Lecture Hall Research II, Jacobs University

**Abstract:**

A “circulant” is a square matrix in which each row is obtained from the previous row by shifting its entries cyclically one step to the right: thus, for an  $n$  by  $n$  matrix the  $i, j$  entry only depends on the value of  $i - j \pmod{n}$ . We will discuss the question of when such a matrix with integer entries is “unimodular” (that is, has determinant either  $+1$  or  $-1$ ). This question arose from group theory, as it determines whether certain so-called “cyclically presented groups” are trivial. The solution involves classical algebra (polynomial resultants), elementary complex arithmetic and inequalities, and — for the hardest case — an application of  $p$ -adic analysis, which is a powerful tool in modern number theory.

**Colloquium Tea** at ca. 16:45 in the Tea Room of Research II, close to the lecture hall. Everybody is welcome!